#### ORIGINAL PAPER

# Estimating tsunami potential of earthquakes in the Sumatra-Andaman region based on broadband seismograms in India

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**Abstract** In this paper, we report that the ratio of broadband energy (0.01–2 Hz) to highfrequency energy (0.3–2 Hz), E<sub>r</sub>, estimated from regional seismograms of India, might be a useful parameter in estimating tsunami potential of earthquakes in the Sumatra-Andaman region.  $E_{\rm r}$  is expected to be sensitive to the depth as well as to the source characteristics of an earthquake. Since a shallow and slow earthquake has a greater tsunamigenic potential,  $E_{\rm r}$  may be a useful diagnostic parameter. We base our analysis on broadband seismograms of the great earthquakes of Sumatra–Andaman (2004,  $M_{\rm w} \sim 9.2$ ) and Nias (2005,  $M_{\rm w}$  8.6), 41 of their aftershocks, and the earthquakes of north Sumatra (2010,  $M_{\rm w}$  7.8) and Nicobar (2010,  $M_{\rm w}$  7.4) recorded at VISK, a station located on the east coast of India. In the analysis, we also included the two recent, great strike-slip earthquakes of north Sumatra (2012,  $M_{\rm w}$  8.6, 8.2) recorded at VISK and three south Sumatra earthquakes (2007,  $M_{\rm w}$  8.5; 2007,  $M_{\rm w}$  7.9; 2010,  $M_{\rm w}$  7.8) recorded at PALK, a station in Sri Lanka. We find that  $E_{\rm r}$  is a function of depth; shallower earthquakes have higher  $E_r$  values than the deeper ones. Thus,  $E_{\rm r}$  may be indicative of tsunamigenic potential of an earthquake. As  $M_{\rm w}$  and  $E_{\rm r}$  increase so does the tsunami potential. In addition to the parameter  $E_r$ , the radiated seismic energy,  $E_s$ , may be estimated from the regional seismograms in India using empirical Green's function technique. The technique yields reliable  $E_{\rm s}$  for the great Sumatra and Nias earthquakes.  $E_{\rm r}$ and  $E_{\rm s}$  computed from VISK data, along with  $M_{\rm w}$  and focal mechanism, may be useful in

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estimating tsunami potential along the east coast of India from earthquakes in the Sumatra–Andaman region in less than  $\sim 20$  min.

**Keywords** Early tsunami warning · Indian Ocean tsunami · 2004 Sumatra earthquake · Radiated energy of Sumatra and Nias earthquakes

#### 1 Introduction

Tsunamis produced by recent great earthquakes of Sumatra–Andaman (December 26, 2004,  $M_{\rm w}$  9.2) and Tohoku-oki (2011,  $M_{\rm w}$  9.1) resulted in unprecedented death and destruction. The tsunami caused by the Sumatra–Andaman earthquake claimed more than 280,000 lives in Indonesia, Thailand, Sri Lanka, and India and left about 1.5 million homeless. To prevent future loss of lives, early tsunami warning systems have been developed and deployed in the region. In particular, India has implemented its own warning system. National Tsunami Early Warning System (NTEWS) has been established at the Indian National Centre for Ocean Information Services (INCOIS), Hyderabad. As part of the effort, a 17-station Real Time Seismic Monitoring Network (RTSMN) has been set up by the India Meteorological Department (IMD) (Dattatrayam et al. 2009). RTSMN and IRIS data are now being routinely used by IMD to determine location and magnitude of earthquakes in the region and to flag those with potential for tsunami (Dattatrayam et al. 2009).

Early tsunami warning systems mostly rely on magnitude and location of an earthquake. A large magnitude earthquake with a location near the trench of a subduction zone is potentially a tsunamigenic event. Appropriate magnitudes for tsunami warning are those that are based on long-period seismic waves (Abe 1979), for example, the moment magnitude,  $M_{\rm w}$  (Kanamori 1977), or the mantle-wave magnitude,  $M_{\rm M}$  (Brune and Engen 1969; Talandier and Okal 1989). Lockwood and Kanamori (2006) showed that W-phase (the long-period wave that arrives between P and S waves) could be retrieved from wavelet analysis that may be useful in quick identification of great earthquakes and high tsunami potential. Presently, W-phase is being routinely used to invert for centroid moment tensor (Kanamori and Rivera 2008; Hayes et al. 2009). This solution is extremely useful for early tsunami alert since it can be determined in a relatively short time. Real-time analysis of near-source GPS data seems very promising in quick estimation of critical source parameters, including  $M_{\rm w}$  (e.g., Singh et al. 2012).

An earthquake that generates disproportionately large tsunami in relation to its surface-wave magnitude,  $M_{\rm s}$ , is denoted as a tsunami earthquake (Kanamori 1972). Mechanisms proposed for such earthquakes include slip on steeply dipping faults in the accretionary prism (Fukao 1979), slumping of sediments near the trench (Ma et al. 1991), and rupture reaching the ocean floor in non-accreting margins where the sediments are subducted along plate interface (Kanamori and Kikuchi 1993). We note that all of these mechanisms involve shallow and possibly slow sources (Polet and Kanmori 2000). Tsunami earthquakes are characterized by large ( $M_{\rm s}-M_{\rm w}$ ) and ( $m_{\rm b}-M_{\rm w}$ ) disparity (Kanamori and Kikuchi 1993) and anomalously low value of  $E_{\rm s}/M_0$  (Newman and Okal 1998; Ammon et al. 2006), where  $m_{\rm b}$  is the short-period body-wave magnitude,  $E_{\rm s}$  is the radiated seismic energy, and  $M_0$  is the seismic moment. Based on these parameters and present state of technology, a rapid detection of a tsunami earthquake is now possible. However, tsunamis are often caused by events that do not qualify as tsunami earthquakes. Although the great earthquakes of 1952 Kamachatka, 1957 Aleutians, 1960 Chile, 1964 Alaska, and 2004 Sumatra produced the five largest tsunamis of the last 100 years, none of these events



qualify as tsunami earthquake. Because of their magnitude and location, such earthquakes should automatically give rise to early tsunami warning. It remains a challenge to assess tsunamigenic potential of events that do not fall in the category of tsunami earthquake but may generate large tsunamis. For example, the Nias earthquake of March 28, 2005 ( $M_{\rm w}$  8.6), generated smaller tsunami in relation to its magnitude (Geist et al. 2006). What parameter, based on seismic data, could have been used to rapidly detect this?

The W-phase CMT solution for earthquakes in the Sumatra–Andaman region is now available in less than 20 min, giving centroid location,  $M_{\rm w}$ , and focal mechanism. These are critical elements toward early tsunami warning. Such a warning would be useful for the east coast of India and Sri Lanka, although not for the near-source region. We expect high tsunami potential from shallow and slow earthquakes. While the W-phase CMT solution yields the centroid depth, it does not provide any information on the details of the source, for example, possible slow slip on the fault. It follows that a parameter that is sensitive to both the depth and the source characteristics and may be estimated rapidly will be useful in estimating tsunami potential.

Shapiro et al. (1998), Iglesias et al. (2003), and Singh et al. (2008) reported that the ratio of total to high-frequency energy,  $E_{\rm r}$ , is a useful parameter in depth discrimination. These studies show that  $E_{\rm r}$  of earthquakes along the Pacific coast of Mexico, recorded on a broadband seismograph in Mexico City (3°  $\leq \Delta \leq$  5°), is sensitive to the depth of the event: Shallower, near-trench events have larger  $E_{\rm r}$  than the deeper ones. This suggests that earthquakes with large  $E_{\rm r}$  may have high tsunamigenic potential. The dependence of  $E_{\rm r}$  on depth arises from the fact that seismograms of shallower events at regional distance are enhanced at longer periods as compared to those of the deeper ones. The method is reminiscent of the work of Tsai and Aki (1970), which showed that surface-wave amplitude spectra could be used to determine focal depth. In fact,  $E_{\rm r}$  includes both the effect of the depth and the source characteristics. In this sense,  $E_{\rm r}$  provides useful complementary information to the centroid depth. In a somewhat similar approach, the energy content in the seismogram estimated from wavelet analysis has been proposed as a diagnostic tool for early tsunami by Chamoli et al. (2010).

Since  $E_{\rm r}$  is a ratio, the effect of focal mechanism is canceled out. If path and distance from different events to a given station are roughly the same (thus requiring only a minor correction to normalize the data to a common distance), then it should be possible to compare  $E_{\rm r}$  values of different earthquakes in a meaningful fashion. In this paper, we explore whether  $E_{\rm r}$ , defined here as the ratio of broadband energy (0.01–2 Hz) to high-frequency energy (0.3–2 Hz), is a useful parameter for assessing tsunami potential. We compute  $E_{\rm r}$  from broadband seismograms of earthquakes in the Sumatra–Andaman region recorded at VISK, a station on the east coast of India ( $\Delta \sim 15$ –25°). We also investigate whether the radiated seismic energy,  $E_{\rm s}$ , of great earthquakes in the region, and hence  $E_{\rm s}/M_0$ , can be estimated rapidly from broadband seismograms recorded at Indian stations using empirical Green's function technique.

# 2 Data

We searched for events in the Sumatra–Andaman region recorded at VISK since 1997, the year the station became operational. The selected events, with good signal-to-noise ratio, consist of earthquake of November 2, 2002 ( $M_{\rm w}$  7.2), the two great earthquakes (December 26, 2004,  $M_{\rm w} \sim 9.2$ ; March 28, 2005,  $M_{\rm w}$  8.6) and 41 of their aftershocks (which occurred before August 12, 2006), north Sumatra earthquake of April 6, 2010 ( $M_{\rm w}$  7.8), and Nicobar



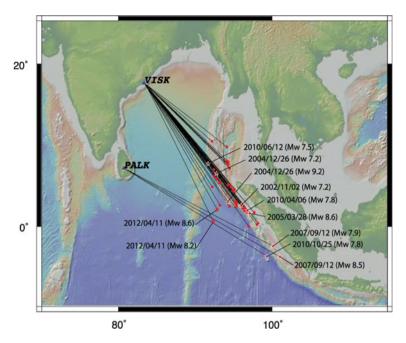


Fig. 1 Map showing stations VISK and PALK and epicenters of earthquakes (dot:  $M_w < 7$ ; star:  $M_w \ge 7$ ). Seismograms at VISK and PALK are used to analyze earthquakes in the Sumatra–Andaman and southern Sumatra regions, respectively. The date and magnitude of large earthquakes ( $M_w \ge 7$ ) are given in the figure

earthquake of June 12, 2010 ( $M_{\rm w}$  7.5) (Fig. 1). The aftershocks of the two great earthquakes that were visibly contaminated by other events were excluded from the analysis.

In the analysis, we also included the two recent, great strike-slip earthquakes of north Sumatra (2012,  $M_{\rm w}$  8.6, 8.2) and south Sumatra earthquakes of September 12, 2007 ( $M_{\rm w}$  8.5,  $M_{\rm w}$  7.9), and October 25, 2010 ( $M_{\rm w}$  7.8). The events are listed in Table 1. The table includes the centroid depths reported in Global CMT catalog. Depth, H, if reported by Engdahl et al. (2007) is also given in the table. In our analysis, H is taken from Engdahl et al. for  $M_{\rm w} < 7$  if available; otherwise, we use the centroid depth. For larger earthquakes ( $M_{\rm w} \ge 7$ ), we use the centroid depth. The epicentral distance of the events in the Sumatra–Andaman and north Sumatra regions from VISK ranges between 1,234 and 2,515 km,  $M_{\rm w}$  ranges between 5.5 and 9.2, and the depth ranges between 10 and 58 km (Table 1). The three south Sumatra earthquakes are located between 2,893 and 3,066 km from VISK. These distances are greater than for the other earthquakes listed in Table 1. For this reason, for the south Sumatra earthquakes, we used data from PALK, which is located at distance between 2,398 and 2,564 km.

# 3 Validation of the method and computation of $E_{\rm r}$

We compute  $E_{\rm r}$  from:

$$E_r = \frac{\int_{f_1}^{f_3} V^2(f) df}{\int_{f_2}^{f_3} V^2(f) df} \tag{1}$$

where  $V^2(f) = V_N^2(f) + V_E^2(f) + V_Z^2(f)$  and  $V_i(f)$  is the Fourier velocity spectrum of *i*-th component, normalized to a common distance. The normalization distance was taken as



Table 1 Earthquakes from Sumatra-Andaman and southern Sumatra regions analyzed in this study

Date Year/M/Day	Time Hr:Min	Lat	Long	H, km <sup>a</sup>	Magnitude <sup>c</sup>	Mechanism $\varphi \delta \lambda$	Station	R, km	$E_{\rm r}$
2002/11/02	01:26	2.65	95.99	23/NA	7.2/7.6	297 16 73	VISK	2,165	8.0e2
2004/12/26	01:01	3.09	94.26	29/30	9.2/8.8	329 8 110	VISK	2,006	5.0e2
2004/12/26	04:21	6.61	92.79	14/15	7.2/7.5	351 27 121	VISK	1,601	1.9e4
2004/12/31	02:24	7.10	92.43	12/12	6.1	319 14 75	VISK	1,534	1.1e3
2004/12/31	12:05	6.03	92.80	12/17	6.0	359 39 143	VISK	1,651	7.5e1
2004/12/31	17:48	4.68	95.09	24/50	5.9	326 3 100	VISK	1,928	2.0e0
2005/01/01	01:55	2.55	95.38	26/26	5.6	305 21 80	VISK	2,130	1.8e1
2005/01/01	06:25	4.99	92.20	12/17	6.6	111 80-177	VISK	1,706	2.6e1
2005/01/01 <sup>d</sup>	19:08	7.27	94.47	34/25	6.1	156 86–178	VISK	1,838	8.1e1
2005/01/02	08:27	3.16	95.30	12/16	5.7	285 50 81	VISK	2,072	2.1e1
2005/01/02 <sup>b</sup>	15:36	6.25	92.47	12/25	6.3	340 28 89	VISK	1,610	5.2e1
2005/01/04	09:13	10.62	92.17	22/25	6.1	353 12 96	VISK	1,234	1.1e1
2005/01/06	00:56	5.07	94.62	51/58	5.7	333 27 110	VISK	1,861	2.0e0
2005/01/09	22:13	4.61	94.89	53/57	6.0	319 25 100	VISK	1,919	2.0e0
2005/01/26	17:30	8.18	94.15	12/19	5.5	165 72-162	VISK	1,576	1.2e1
2005/01/26 <sup>d</sup>	22:00	2.51	94.44	12/16	5.9	306 31 78	VISK	2,073	1.7e2
2005/01/27	16:58	7.79	94.28	13/22	5.7	237 82 4	VISK	1,616	1.3e2
2005/01/27	18:52	7.83	94.26	15/10	5.5	144 80-178	VISK	1,611	1.1e2
2005/01/28	07:49	7.85	94.20	12/18	5.5	141 70–176	VISK	1,605	6.2e1
2005/02/02	01:30	9.93	94.10	12/25	5.5	247 58-62	VISK	1,447	2.4e1
2005/02/03	04:51	5.59	93.27	39/40	5.5	286 86 162	VISK	1,722	1.0e0
2005/02/05	17:35	8.07	94.27	12/10	5.9	91 80 5	VISK	1,594	1.1e2
2005/02/09 <sup>d</sup>	13:27	4.48	94.97	50/53	6.0	316 24 95	VISK	1,936	6.0e0
2005/02/17	05:31	4.40	95.01	51/54	5.6	307 28 88	VISK	1,945	2.0e0
2005/02/18	19:33	5.26	94.25	44/45	5.6	327 28 106	VISK	1,818	3.0e0
2005/02/25	13:31	7.67	94.24	12/21	5.6	240 89 14	VISK	1,622	3.3e1
2005/02/26	12:56	2.84	95.38	12/23	6.7	297 6 72	VISK	2,105	2.5e2
2005/03/28	16:10	1.67	97.07	26/30	8.6/8.4	333 8 118	VISK	2,320	4.8e3
2005/03/29	05:16	2.30	96.3	40/40	5.9	309 24 108	VISK	2,216	1.1e1
2005/03/30 <sup>b</sup>	16:19	2.87	95.24	12/25	6.4	305 7 82	VISK	2,094	7.4e1
2005/04/03	00:59	0.23	98.04	37/38	6.0	330 19 112	VISK	2,515	6.0e0
2005/04/03	03:11	1.75	97.67	49/50	6.3	326 23 110	VISK	2,360	8.0e0
2005/04/11	06:11	1.95	96.42	27/29	6.1	314 14 89	VISK	2,254	2.5e1
2005/04/28 <sup>b</sup>	14:07	1.91	96.49	17/31	6.3	310 10 86	VISK	2,262	2.6e1
2005/05/14	05:05	0.42	98.18	41/40	6.7	327 20 90	VISK	2,509	3.2e1
2005/05/18	11.37	5.53	93.17	38/35	6.1	281 83 153	VISK	1,720	2.0e0
2005/05/19	01:55	2.00	96.74	12/25	6.9	297 7 75	VISK	2,272	9.3e1
2005/05/21	23:01	5.10	94.60	52/45	5.6	334 28 110	VISK	1,857	2.0e0
2005/11/19 <sup>b</sup>	14:10	2.04	96.55	12/NA	6.4	311 9 85	VISK	2,255	5.6e1
2006/04/19	20:36	2.70	93.22	17/NA	6.2	111 66–176	VISK	1,980	5.1e1
2006/04/25	18:26	1.78	96.77	12/NA	6.3	293 7 66	VISK	2,294	2.4e2



Date Year/M/Day	Time Hr:Min	Lat	Long	H, km <sup>a</sup>	Magnitude <sup>c</sup>	Mechanism $\varphi \delta \lambda$	Station	R, km	$E_{\rm r}$
2006/05/16	15:28	0.01	96.98	14/NA	6.8	358 82–31	VISK	2,462	2.8e2
2006/08/11	20:54	2.31	96.17	21/NA	6.2	310 9 88	VISK	2,206	2.6e2
2007/09/12	11:11	-3.78	100.99	24/NA	8.5/8.5	328 9 114	PALK	2,564	1.5e5
2007/09/12	23:49	-2.46	100.13	43/NA	7.9/8.1	317 19 102	PALK	2,415	1.7e4
2010/04/06	22:15	2.07	96.74	18/NA	7.8/7.9	307 7 88	VISK	2,266	2.9e3
2010/06/12	19:27	7.85	91.65	33/NA	7.5/7.5	220 66 32	VISK	1,416	2.9e2
2010/10/25	14:43	-3.71	99.32	12/NA	7.8/7.8	316 8 96	PALK	2,398	5.0e4
2012/04/11	08:39	2.24	92.78	40/NA	8.6	20 64 1	VISK	2,000	2.8e3
2012/04/11	10:43	0.76	92.25	54/NA	8.2	16 74-10	VISK	2,114	2.1e3

Table 1 continued

2,000 km, which is roughly the distance of VISK from the hypocenters of the great 2004 earthquake and many of its aftershocks. The procedure of normalization is described in Appendix A. The time window used in the analysis began with the arrival of S wave and had a duration of  $\sim 1,500$  s. (Test shows that  $\sim 900$  s of signal may suffice.) The signals were Fourier-transformed, smoothed with a 1/6 octave-band filter, and 5 % tapered.

The upper limit of the integration in Eq. 1,  $f_3$ , was taken as 2 Hz. This ensured that the spectra were above the noise at the high-frequency end for all events considered in this study. Our choice of  $f_3 = 2$  Hz was also guided by the fact that the normalization to a common distance leads to greater uncertainty at high frequencies. The lower limit of integration in the numerator,  $f_1$ , was taken as 0.01 Hz. This is the smallest frequency above which the spectra of all events were above noise. We set the lower limit in the denominator ( $f_2$ ) as 0.3 Hz. Thus, in Eq. 1, the numerator and the denominator are proportional to broadband and high-frequency energy, respectively.

Figure 2 shows broadband seismograms of three aftershocks ( $M_{\rm w} \sim 6$ ) of the great Sumatra 2004 earthquake recorded at VISK at a distance of  $\sim 2,000$  km. The depths of the events are 16 km, 25 km, and 53 km. The velocity spectra of these events are shown in Fig. 3. As these two figures illustrate, the shallow earthquake is enriched at long periods as compared to the deeper events. The spectra suggest that, for earthquakes of same  $M_{\rm w}$ , the ratio of broadband to high-frequency energy,  $E_{\rm r}$ , will be greater for the shallower event as compared to the deeper one.

#### 4 Dependence of $E_{\rm r}$ on $M_{\rm w}$

We expect the computed  $E_r$  to be a function of depth. However, since source spectrum depends on the size of the earthquake while the limits of integration in Eq. 1 are fixed for all events,  $E_r$  will also be a function of  $M_w$ . To correctly interpret the results, it is useful to establish the theoretical dependence on  $E_r$  on  $M_w$ . For this purpose, we computed  $E_r$ 



<sup>&</sup>lt;sup>a</sup> First and second numbers refer to depths reported in Gobal CMT catalog and Engdahl et al. (2007), respectively

<sup>&</sup>lt;sup>b</sup> Events chosen for the estimation of Q (see Appendix A) <sup>c</sup> First and second numbers refer to magnitudes  $M_{\rm w}$  and  $M_{\rm s}$ , respectively. If  $M_{\rm w} < 7$ , then only  $M_{\rm w}$  is listed

<sup>&</sup>lt;sup>d</sup> Events whose spectra are compared in Fig. 2

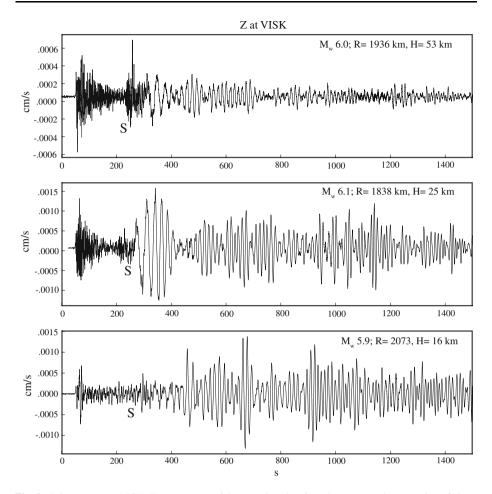


Fig. 2 Seismograms at VISK (Z component) of three earthquakes from Sumatra–Andaman region of about the same magnitude ( $M_{\rm w} \sim 6$ ) but different depth. The epicentral distance of these events is nearly equal. Note the relative enrichment of high-frequency signal of deeper events (*top* and *middle traces*) as compared to the shallow event (*bottom trace*). S-wave arrival is marked by letter S

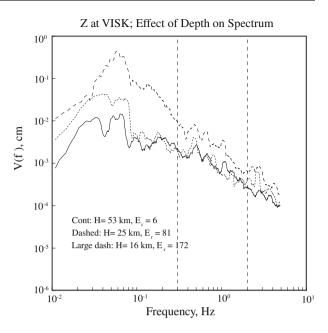
assuming an  $\omega^2$  source model. In this case, V(f) in Eq. 1 is proportional to  $f\dot{M}_0(f)e^{-\pi fR/UQ}$ , where  $\dot{M}_0(f) = M_0 f^2/(f^2 + f_c^2)$  is the moment rate spectrum,  $f_c$  is the corner frequency, U is the group velocity (assumed here as 3.5 km/s), R is the hypocentral distance, and Q is the quality factor (Appendix A). In computing  $E_r$ , we assumed the Brune source model (Brune 1970) and a constant stress drop  $(\Delta\sigma)$  of 10 MPa.

#### 4.1 $E_{\rm r}$ versus $M_{\rm w}$

Figure 4 shows  $E_r$  versus  $M_w$  plot for earthquakes in the Sumatra–Andaman region. In the figure, events with depth H < 25 km,  $25 \le H < 40$  km, and  $H \ge 40$  km are marked by circles, dots enclosed by circles, and dots, respectively. In most cases, for the same  $M_w$ , the shallower events have higher  $E_r$  values than the deeper ones. Although the depth range of the events varies by a factor of about 6 (10–58 km; Table 1),  $E_r$  for the same  $M_w$  varies by



Fig. 3 Velocity spectra of the earthquakes shown in Fig. 2. Time window taken in the computation of the spectra is  $\sim 1.500$ -s long. Spectrum of shallow earthquake is enriched at long periods as compared to the deeper events. This suggest that, for earthquakes of same  $M_{\rm w}$ , the ratio of broadband to highfrequency energy,  $E_r$ , will be greater for the shallower event as compared to the deeper one. Computed  $E_{\rm r}$  values are 172, 81, and 6 for events of depths 16, 25, and 53 km, respectively (Table 1)



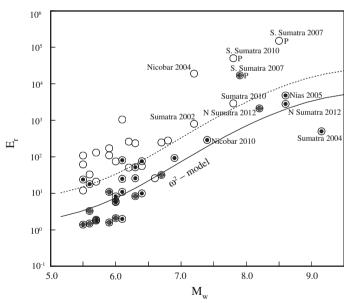


Fig. 4  $E_{\rm r}$  versus  $M_{\rm w}$  for earthquakes of Sumatra–Andaman region.  $E_{\rm r}$  of these events is computed from seismograms at VISK.  $E_{\rm r}$  of three large/great earthquakes from southern Sumatra region, computed from data at PALK, is also shown. Circle: H < 25 km; dot with circle:  $25 \le H < 40$  km; dot:  $H \ge 40$  km. For  $M_{\rm w} < 7.0$ , H is taken from Engdahl et al. (2007) if available; otherwise, it is from Global CMT catalog (Table 1). For  $M_{\rm w} \ge 7.0$ , H is the centroid depth. These events are identified in the figure. P: PALK. In general,  $E_{\rm r}$  decreases with increasing depth. The continuous reference curve, based on  $\omega^2$  source model, divides the events with H < 40 km from deeper events. The dashed reference curve, whose ordinates are 4.5 times greater than that of the continuous reference curve, divides H < 25 km events from deeper ones



a factor of more than 100. Larger  $E_r$  for shallower earthquakes may be attributed to more efficient excitation of long-period surface-waves and possible slower nature of the shallower sources. Figure 4 also shows theoretically expected  $E_r$  versus  $M_w$  curve based on the  $\omega^2$  Brune source model with constant stress drop (10 MPa) (continuous curve). For convenience, we also show a dashed curve whose ordinate is shifted 4.5 times with respect to the continuous curve. Henceforth, we will call these two curves the reference curves. Increase in  $E_r$  with  $M_w$ , seen in the data, is in accordance with the shape of the reference curves. In general, the dashed and continuous reference curves separate events with depth H < 25 km,  $25 \le H < 40$  km, and  $H \ge 40$  km events fairly well. Figure 4 is encouraging: An earthquake in the Sumatra–Andaman region for which  $E_r$  at VISK falls above the dashed reference curve is very likely to be shallow in depth.

We note the following points in relation to earthquakes with  $M_{\rm w} \ge 7$  (Fig. 4):

- (1)  $E_{\rm r}$  of earthquakes of Sumatra in 2002 ( $M_{\rm w}$  7.2) and Nicobar in 2004 ( $M_{\rm w}$  7.2) and 2005 ( $M_{\rm w}$  7.2) are above the dashed reference curve. The centroid depths of these earthquakes are also less than 25 km. It is not known whether these earthquakes generated appreciable tsunami.
- (2)  $E_{\rm r}$  at VISK for the 2005 Nias earthquake ( $M_{\rm w}$  8.6) is slightly below the dashed reference curve. This is not surprising. It has been suggested that the tsunami generation during this event was deficient in relation to its magnitude (e.g., Geist et al. 2006). A likely explanation for the relatively small  $E_{\rm r}$  value and deficient tsunami generation is offered by the concentration of slip in the downdip part of the rupture area (Ammon et al. 2005; Ji 2005; Geist et al. 2006).
- (3) E<sub>r</sub> at VISK of the northern Sumatra earthquake of April 6, 2010 (M<sub>w</sub> 7.8), is slightly above the dashed curve indicating shallow source. This agrees with the Global CMT depth of 20 km. E<sub>r</sub> and M<sub>w</sub> values of this earthquake suggest a tsunamigenic earthquake. However, the water depth at the epicenter is only 19 m. Based on the shallow water depth and pre-run model scenarios, INCOIS correctly issued a bulletin within about 37 min of the origin time, stating that there was no tsunami threat to India. The event demonstrates why availability of several key parameters is useful in correctly assessing tsunami potential of an earthquake.
- (4) For the Nicobar earthquake of 2010 (M<sub>w</sub> 7.4), E<sub>r</sub> at VISK points to a source depth between 25 and 40 km. This is in agreement with the Global CMT depth of 37 km, suggesting a non-tsunamigenic earthquake. INCOIS, initially, issued a tsunami watch report, which was canceled about 1 h 32 min after the origin time of the earthquake, as the tide gauge at Andaman did not show any significant change.
- (5)  $E_{\rm r}$  values of the three southern Sumatra earthquakes are also plotted in Fig. 4. Since these have been computed from PALK recordings, these values are not directly comparable with the others in the figure. It is reassuring, however, that  $E_{\rm r}$  of the shallower earthquakes of September 12, 2007, 11:11 ( $M_{\rm w}$  8.5, H=25 km) and October 25, 2010 ( $M_{\rm w}$  7.9, H=12 km), are higher with respect to the dashed reference curve than that of the deeper earthquake of September 12, 2007, 23:49 ( $M_{\rm w}$  7.9, H=43 km). The tsunami caused by the earthquake of 2010 killed about 500 persons in Pagai Island. Tsunami alert was issued by the Pacific Tsunami Warning Centre and Indian authorities following the 2007,  $M_{\rm w}$  8.5 earthquake. A 1-m-high tsunami was recorded at Padang Island.
- (6)  $E_{\rm r}$  at VISK for the great 2004 Sumatra earthquake ( $M_{\rm w}$  9.2) is well below the continuous reference curve. This is intriguing. Why is  $E_{\rm r}$  so low for this great earthquake, which generated such large tsunami and caused unprecedented loss? Below we address this issue.



(7)  $E_r$  values at VISK of the two recent, great, and extremely unusual strike-slip earthquakes offshore north Sumatra (2012,  $M_w$  8.6, 8.2) fall between dashed and continuous curves, suggesting that the depth of significant slip was located between 25 and 40 km. Thus, the strike-slip focal mechanisms reported in the W-phase CMT solution and the low  $E_r$  values would have indicated a low tsunamigenic potential for both of these events. The centroid depths of the two events, as reported in the GCMT catalog, are 40 and 54 km, respectively (Table 1); the corresponding CMT depths given by U.S. Geological Survey are 40 and 43 km. These depths are somewhat greater than those inferred from the  $E_r$  values (between 25 and 40 km). We note that the centroid depths, reported by National Earthquake Information Center, U.S. Geological Survey, from the W-phase inversion are 25 and 16 km. Thus, the depth of significant slip during these earthquakes is, as yet, uncertain. Based on magnitude and location of the first great earthquake and pre-run modeling, INCOIS declared several zones to be potentially under tsunami threat. Only minor tsunamis were observed at several locations.

## 4.2 Low $E_r$ for the great Sumatra earthquake ( $M_w$ 9.2)

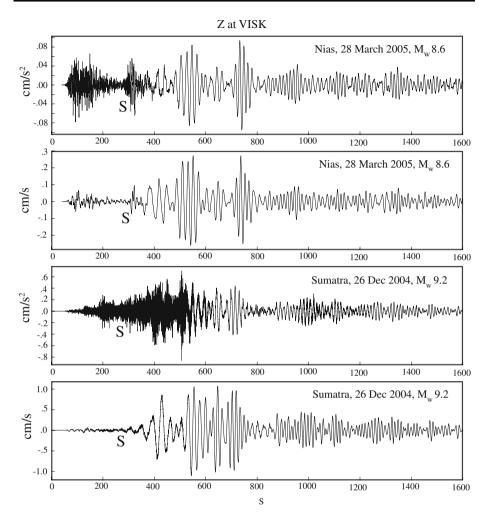
An inspection of VISK recordings provides one possible cause of the relatively low value of  $E_r$ . Velocity and acceleration traces at VISK of the Sumatra ( $M_w$  9.2) and the Nias earthquake ( $M_{\rm w}$  8.6) (Z component) are shown in Fig. 5. Various studies demonstrate that the rupture during the Sumatra earthquake lasted  $\sim 600 \text{ s}$  (e.g., Ni et al. 2005; Ishii et al. 2005; Ammon et al. 2005; de Groot-Hedlin 2005). As a consequence, high-frequency P waves overlap with S waves and the beginning of surface waves. This is clearly seen from a comparison of acceleration and velocity traces of the event (Fig. 5). For the Nias earthquake, the S waves are well separated from the P waves and their coda. The velocity Fourier spectra of these two events are shown in Fig. 6. As the time window used in the analysis begins at the arrival of S waves, the signal of the Sumatra earthquake includes high-frequency P waves. It gives rise to slow spectral falloff at f > 0.2 Hz, and the corresponding increase in high-frequency energy results in small value of  $E_{\rm r}$  (Eq. 1). Small value of  $E_r$  for this great earthquake, however, does not argue against  $E_r$  being a useful parameter for early tsunami warning, because, first, such long-duration, great-magnitude event is infrequent and, second, such great-magnitude earthquake and its location merit early tsunami warning irrespective of the  $E_r$  value.

#### 5 Rapid estimation of radiated energy, $E_s$ , of great earthquakes

As mentioned above, tsunami earthquakes are characterized by an anomalously low value of  $E_s/M_0$  (e.g., Newman and Okal 1998; Venkataraman and Kanamori 2004; Ammon et al. 2006), where  $E_s$  is the radiated seismic energy. Here, we test whether rapid and reliable estimation of  $E_s$ , hence of  $E_s/M_0$ , of earthquakes in Sumatra–Andaman region is possible in an operational mode using broadband seismograms from India. We note that the stations of India lie within the distance range about  $15^{\circ}-25^{\circ}$  from Sumatra–Andaman earthquakes. For this reason, methods based on teleseismic P-wave group (e.g., Boatwright and Choy 1986) may not be suitable for the estimation of  $E_s$ .

An alternative is to use the empirical Green's function (EGF) technique (e.g., Venkataraman et al. 2002; Singh et al. 2004). Recordings of a smaller earthquake from the same





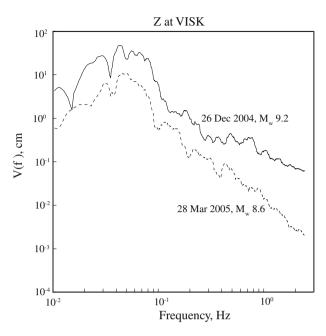
**Fig. 5** Velocity and acceleration traces (Z component) of December 26, 2004 ( $M_{\rm w}$  9.2), and March 28, 2005 ( $M_{\rm w}$  8.6), earthquakes recorded at VISK. S-wave arrival is marked by letter S

region can be used as EGF provided that the location and focal mechanism of the EGF and the larger, target event are similar. The method has the advantage that it does not require corrections for attenuation and local site effects. The magnitude of the target event, however, should be at least two units greater than that of the EGF. Assuming point-source, far-field approximation to be valid,  $E_s$  can be written as (Vassiliou and Kanamori 1982):

$$E_{\rm s} = \frac{4\pi}{5\rho\beta^5} \int_0^\infty f^2 \dot{M}^2(f) df \tag{2}$$

where  $M_0(f)$  is the moment rate spectrum, and  $\rho$  is the density, and  $\beta$  is the shear-wave velocity in the source region. Let us assume that the seismogram of an appropriate smaller-magnitude earthquake is available such that it can be used as an EGF for the mainshock.





**Fig. 6** Fourier velocity spectra of December 26, 2004 ( $M_{\rm w}$  9.2), and March 28, 2005 ( $M_{\rm w}$  8.6), earthquakes recorded at VISK. The time window used in the computation of spectra begins with the arrival of S wave and is  $\sim 1,500$  s long

The moment rate spectrum of the mainshock can then be approximated from the ratio of the spectrum of the mainshock to the EGF and multiplying the ratio by  $M_0$  of the EGF event. This approximation is valid at frequencies smaller than the corner frequency of the EGF. Earthquakes with  $M_{\rm w} \ge 6.0$  in Sumatra-Andaman region produce seismograms in India with acceptable signal-to-noise ratio in the frequency band of interest, so they are likely candidates to be used as EGF. For rapid estimation of Es using the EGF technique, we would like to set, a priori, the upper limit of integration, in Eq. 2, to a fixed value, say,  $f_{\rm u}$ , which is smaller than the corner frequency of the EGF. For EGF and mainshock whose moment- magnitudes are  $\sim 6$  and  $\geq 8$ , respectively, a reasonable choice of  $f_u$  is 0.1 Hz. The contribution to  $E_s$  of frequencies greater than  $f_u$ , can be obtained by assuming an  $f^{-2}$ falloff of moment rate spectrum,  $\dot{M}_0(f)$ , beyond  $f_u$ . This contribution is given by  $(4\pi/5\rho\beta^5) f_u^3 \dot{M}_0^2(f_u)$ . In our case, we set the lower limit of integration,  $f_1$ , in Eq. 2 at 0.005 Hz. The signal is above noise at frequencies ≥0.005 Hz for the EGF events. We will assume that the corner frequency of the mainshock is greater than 0.005 Hz. In this case, the contribution to  $E_{\rm s}$  from the frequency range 0-0.005 Hz is given by  $(4\pi/5\rho\beta^5)$   $(f_l^3/3)M_0^2$ , where  $f_1 = 0.005$  Hz. This contribution to  $E_s$  is negligible as compared to that from f > 0.005 Hz.

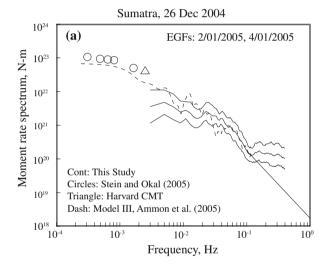
The precise depth extent of the mainshock rupture will, of course, be unknown immediately after the earthquake. In computing  $E_{\rm s}$ , we will take  $\rho=3.2$  gm/cm<sup>3</sup> and  $\beta=4.62$  km/s, appropriate for upper mantle structure. If the true values are  $\rho_{\rm t}$  and  $\beta_{\rm t}$ , then the computed  $E_{\rm s}$  needs to be multiplied by a factor  $(3.2/\rho_{\rm t})(4.62/\beta_{\rm t})^5$ .

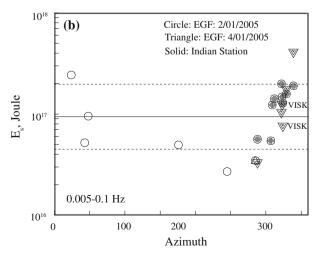


# 5.1 Sumatra earthquake of January 26, 2004

The point-source approximation is violated by the great Sumatra earthquake, whose rupture length was ~1,400 km (e.g., Ammon et al. 2005). We, nevertheless, assume that Eq. 2 can be used for rough estimation of  $E_s$ . We used aftershocks of January 2, 2005 (6.25°N, 92.47°E;  $M_w$  6.4), and January 4, 2005 (10.62°N, 92.17°E;  $M_w$  6.1), as EGFs (Table 1). Figure 7a shows  $\dot{M}_0(f)$  of the Sumatra earthquake retrieved from the EGF technique (continuous curve). The figure includes  $\dot{M}_0(f)$  reported by Stein and Okal (2005) at ultra-low frequencies and in Global Centroid Moment-Tensor (GCMT) catalog at about 0.0025 Hz. It also shows  $\dot{M}_0(f)$  computed from the source time function of model III of Ammon et al. (2005). We note that  $\dot{M}_0(f)$  from the EGF technique and from model III is fairly consistent in the frequency range of 0.005–0.1 Hz. We computed  $E_s$  in this frequency band using Eq. 2. The result is shown in Fig. 7b as a function of azimuth. For the entire

Fig. 7 a Median and  $\pm 1$ standard deviation curve of moment rate spectrum,  $\dot{M}_0(f)$ , of the great 2004 Sumatra earthquake retrieved from the EGF technique (continuous line). Circles:  $\dot{M}_0(f)$  reported by Stein and Okal (2005) at ultra-low frequencies. Triangle: Mo reported in Global Centroid Moment-Tensor (GCMT) catalog (triangle).  $\dot{M}_0(f)$  computed from the source time function of model III of Ammon et al. (2005) is shown by dashed line. Straight line shows  $f^{-2}$  falloff of  $\dot{M}_0(f)$  at f > 0.1 Hz. **b**. Radiated seismic energy,  $E_s$ , in the frequency band 0.005-0.1 Hz, plotted as a function of azimuth. Solid symbols show stations in India. Horizontal lines show median and  $\pm 1$  standard deviation value of  $E_s$ 



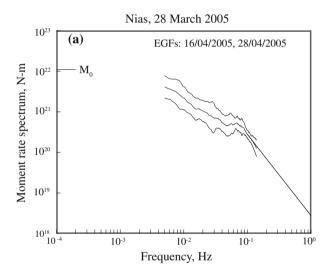


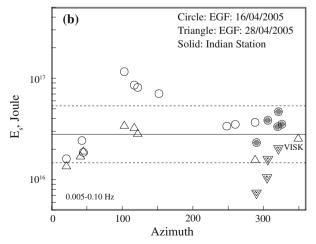


data set,  $\log E_{\rm s}=16.974\pm0.320$ , which gives a median  $E_{\rm s}=9.42\times10^{16}$  J.  $E_{\rm s}$  in the frequency band 0–0.005 Hz is  $7.0\times10^{15}$  J. Median  $\dot{M}_0(f_u)$  at  $f_{\rm u}=0.1$  Hz is  $1.74\times10^{20}$  N-m (Fig. 7). This yields  $E_{\rm s}=1.12\times10^{16}$  J for f>0.1 Hz. Thus, our estimate of total  $E_{\rm s}$  is  $1.12\times10^{17}$  J. We note that  $E_{\rm s}$  estimated from the Indian stations (shown by solid symbols in Fig. 7), as well as from VISK alone, is close to this value. For comparison, Choy and Boatwright (2007) and Kanamori (2006) report  $E_{\rm s}=1.4\times10^{17}$  J and  $3.0\times10^{17}$  J, respectively. These values are close to the one reported here. Our estimate of  $E_{\rm s}$  differs from that by Kanamori (2006) mostly at f>0.1 Hz:  $1.11\times10^{16}$  J versus  $1.6\times10^{17}$  J. We recall that our estimation of  $E_{\rm s}$  in the frequency band  $0.1-\infty$  Hz relies on the assumption of  $f^{-2}$  falloff of the moment rate spectrum, while Kanamori's (2006) estimate uses observed seismograms, and, hence, it may be more reliable.

From  $E_{\rm s}=1.12\times 10^{17}~{\rm J}$  and  $M_0=1.2\times 10^{23}~{\rm N}$  m, we obtain  $E_{\rm s}/M_0=1.0\times 10^{-6}.$  If we consider the range of the reported values of  $E_{\rm s}$  (1.12–3.0 × 10<sup>17</sup> J) and  $M_0$  (0.6–1.3 × 10<sup>23</sup> N m), then  $E_{\rm s}/M_0$  ranges between 1.1 × 10<sup>-6</sup> and 5.0 × 10<sup>-6</sup>. These

Fig. 8 a Median and  $\pm$  1 standard deviation curve of moment rate spectrum,  $\dot{M}_0(f)$ , of the great 2005 Nias earthquake retrieved from the EGF technique (continuous line). Straight line shows  $f^-$ 2 falloff of  $\dot{M}_0(f)$  at f > 0.1 Hz. b Radiated seismic energy,  $E_{\rm s}$ , in the frequency band 0.005-0.1 Hz, plotted as a function of azimuth. Solid symbols show stations in India. Horizontal lines show median and  $\pm$ 1 standard deviation value of  $E_{\rm s}$ 







values are only somewhat smaller than that of other large/great subduction zone earth-quakes (Venkataraman and Kanamori 2004).

## 5.2 Nias earthquake of March 28, 2005

To estimate  $E_{\rm s}$  of Nias earthquake of 2005 ( $M_{\rm w}$  8.6), we took aftershocks of April 16, 2005 (1.67°N, 97.46°E;  $M_{\rm w}$  6.4), and April 28, 2005 (1.91°N, 96.49°E;  $M_{\rm w}$  6.3), as the EGFs. Figure 8a shows  $\dot{M}_0(f)$  of the earthquake retrieved from the EGF technique (continuous curve). Figure 8b shows  $E_{\rm s}$  as a function of azimuth. For the entire data set,  $\log E_{\rm s} = 16.447 \pm 0.281$ , which gives median  $E_{\rm s} = 2.80 \times 10^{16}$  J. Median  $\dot{M}_0(f_u)$  at  $f_u = 0.1$  Hz is  $2.77 \times 10^{20}$  N-m (Fig. 8). This yields  $E_{\rm s} = 1.90 \times 10^{16}$  J for f > 0.1 Hz. Thus, the total  $E_{\rm s}$  is  $4.70 \times 10^{16}$  J. Again,  $E_{\rm s}$  estimated from the Indian stations (shown by solid symbols in Fig. 8) and from VISK alone is close to this value. For this earthquake, Kanamori (2006) and Choy and Boatwright (2007) report  $E_{\rm s}$  of 7.5  $\times$  10<sup>16</sup> J and 6.7  $\times$  10<sup>16</sup> J, respectively. With  $M_0 = 1.1 \times 10^{22}$  N m,  $E_{\rm s}/M_0$  values range between 4.3 and 6.8  $\times$  10<sup>-6</sup>.

We note that our estimated  $E_{\rm s}$  for f>0.1 Hz of this earthquake is greater than that of the great 2004 earthquake:  $1.90\times 10^{16}$  J versus  $1.11\times 10^{16}$  J. The reason is that the median  $\dot{M}_0(f_u)$  at  $f_u=0.1$  Hz of the Nias earthquake (Fig. 8) is greater than that of the 2004 earthquake (Fig. 7). It is possible that our assumption of  $f^{-2}$  falloff at f>0.1 Hz for both earthquakes is not true, and  $E_{\rm s}$  for the great 2004 earthquake, in fact, was greater than for the Nias earthquake in this frequency band.

We have shown above that EGF technique can be used to obtain a reliable estimate of radiated energy of great earthquakes in Sumatra-Andaman region recorded at stations in India. Generally, EGFs of  $M_{\rm w} \geq 6.0$  are needed for adequate signal-to-noise ratio in the frequency band of interest. This constrains the magnitude of the target event to  $M_{\rm w} \geq 8.0$ .

For rapid estimation of  $E_s$  of a great earthquake in the Sumatra–Andaman region using the EGF technique, it will be critical to store recordings of moderate earthquakes along with their locations,  $M_0$ , depths, corner frequencies, and focal mechanisms in computer archives so that one or more appropriate EGF can be immediately retrieved once location and centroid moment tensor of the target event is determined.

#### 6 Discussion and conclusions

In this paper, we have explored the ratio of broadband (0.005–2 Hz) to high-frequency energy (0.3–2 Hz),  $E_{\rm r}$ , computed from regional seismograms recorded at VISK, as an additional parameter to assess the depth and the source characteristics and, hence, tsunami potential of earthquakes in the Sumatra–Andaman region. VISK is located on the east coast of India. The result shows that for moderate earthquakes ( $M_{\rm w} < 7.0$ ),  $E_{\rm r}$  is greater for the shallower ones than for the deeper ones. A reference curve based on  $\omega^2$  source model, shown by the dashed line in Fig. 4, separates shallower earthquakes (H < 25 km) from the deeper ones. Extrapolation of the trend of  $E_{\rm r}$  data of moderate earthquakes suggests that large/great earthquakes with  $E_{\rm r}$  values above the dashed reference curve may have shallow centroid depth. The converse would be true if  $E_{\rm r}$  is below the curve.  $E_{\rm r}$  values of large/great earthquakes at VISK from Sumatra–Andaman region are, indeed, above the dashed reference curve for centroid depths <25 km and below it for depths  $\geq$ 25 km. We find that earthquakes whose  $E_{\rm r}$  values fall below the dashed curve did not produce appreciable tsunami. Consider, for example, the 2005 Nias ( $M_{\rm w}$  8.6) earthquake. Relatively low  $E_{\rm r}$  of



this earthquake at VISK is in agreement with the slip being concentrated on the downdip part of the rupture area (Ji 2005). This earthquake caused smaller local tsunami than expected for its magnitude (e.g., Geist et al. 2006). Low  $E_r$  value for the 2010 Nicobar ( $M_w$ 7.4) earthquake also agrees with the minor tsunami or lack of it for this event. Great magnitude ( $M_{\rm w}$  7.8) and  $E_{\rm r}$  above the dashed curve for the Sumatra 2010 earthquake point to a tsunamigenic earthquake. In this case, shallow water depth above the source area was the reason why no appreciable tsunami was reported. Unexpectedly,  $E_r$  at VISK is low for the 2004 Sumatra-Andaman earthquake ( $M_{\rm w}$  9.2). In this case, the reason, at least partly, appears to be large rupture duration ( $\sim 600 \text{ s}$ ). This causes high-frequency P waves to contaminate S and surface waves used in the computation of  $E_r$ , and give rise to a low  $E_r$ value. However, we are not discouraged by this failure: an  $M_{\rm w}$  9.2 earthquake, located near a trench, merits a tsunami alert irrespective of its  $E_r$  value. Low  $E_r$  values of the two recent, great, strike-slip earthquakes offshore north Sumatra (2012, M<sub>w</sub> 8.6, 8.2) suggests low tsunamigenic potential. This is in agreement with the observed small tsunami, although the strike-slip fault mechanism, involving small vertical sea-floor displacement, must also have played a critical role. In summary, based on physical ground, it is reasonable to assign a higher tsunamigenic potential to earthquakes with values of  $E_{\rm r}$  above the reference curve, even though the available data on tsunami in the region since 1997, when VISK became operational, are too limited to provide its confirmation.

Seeking confirmation of  $E_{\rm r}$  as a useful parameter for assessing tsunami potential, we supplemented the Sumatra–Andaman data with those from three large/great earthquakes of the southern Sumatra region recorded at PALK. The difference in the path requires caution in comparing these data with those from VISK. These earthquakes, nevertheless, support the hypothesis that earthquakes with larger  $E_{\rm r}$  values have greater tsunamigenic potential.

 $E_{\rm r}$  bears similarity with the parameter  $(E_{\rm s}/M_0)$ . Abnormally high  $E_{\rm r}$  and low  $(E_{\rm s}/M_0)$  are both measures of relatively low excitation of high-frequency radiation. An advantage of  $E_{\rm r}$  may be its higher sensitivity to depth and lower sensitivity to detailed source characteristics as compared to that of the parameter  $(E_{\rm s}/M_0)$ . A disadvantage of  $E_{\rm r}$  is that data from other stations and regions cannot be directly compared with those from VISK.

We conclude that the estimation of  $E_r$  using data at VISK, along with the W-phase CMT solution, would be useful in assessing the tsunami potential of earthquakes in the Sumatra–Andaman region. Additionally, the parameter  $(E_s/M_0)$  of great earthquakes could be estimated using regional seismograms from India stations using empirical Green's function technique. These parameters, along with  $(M_s - M_w)$  or  $(m_b - M_w)$  disparity, should lead to a more robust early tsunami warning system for the region.

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#### Appendix A

Normalization of observed spectra to a common distance of 2,000 km

The epicentral distance from VISK to Sumatra–Andaman events, listed in Table 1, varies between 1,100 and 2,515 km (Table 1, Fig. 1). Before computing  $E_r$ , the observed spectra must be reduced to a common distance. This distance has been chosen as 2,000 km. To normalize the spectra, we assume that geometrical spreading and anelastic attenuation are

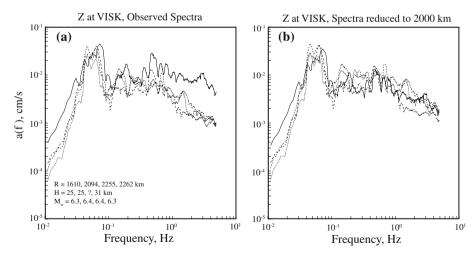


given by  $R^{-1/2}$  (surface waves) and  $e^{\frac{-\pi R}{pQ(f)}}$ , respectively, where R is the hypocentral distance, U is the group velocity (taken here as 3.5 km/s), f is the frequency, and Q(f) is the quality factor. We selected four shallow events of nearly the same magnitude ( $M_{\rm w}$  6.3–6.4), located in the distance range of 1,610 and 2,262 km (Table 1). Global CMT depths of these events are 12 km. The depths of only three of these events have been determined by Engdahl et al. (2007). They lie between 25 and 31 km (Table 1). We assume that the source spectra of these events are the same. Figure 9 shows velocity spectra (Z component) of the four events. We attribute the difference in the spectra to geometrical spreading and anelastic attenuation. Under these assumptions, the spectral ratio of event i with respect to a reference event r at VISK may be written as:

$$[V_i(f)/V_r(f)] = (R_r/R_i)^{1/2} e^{-\pi f(Ri - Rr)/UQ(f)}$$
(3)

The earthquake closest to VISK (2005/01/02; 15:36; R = 1,610 km; Table 1) was taken as the reference event. We take logarithm of both sides of Eq. 3 and compute  $Q^{-1}(f)$  at selected frequencies.  $Q^{-1}(f)$  was computed for the geometrical mean of the spectral amplitudes of the two horizontal components and the vertical component separately.

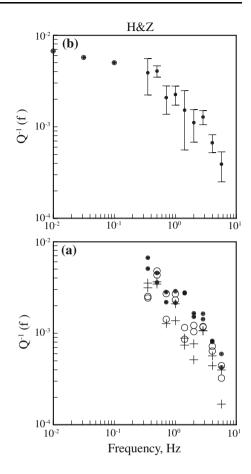
Figure 10 shows  $Q^{-1}(f)$  for each of the three events at discrete frequencies in the range 0.3–5 Hz, while Fig. 10 shows the mean value and  $\pm$  1 standard deviation of  $Q^{-1}(f)$ . The method leads to unreliable results at lower frequencies.  $Q^{-1}(f)$  at these frequencies, shown in Fig. 10, were estimated by fixing its value as 0.0067 at 0.01 Hz (Ben-Menahem 1965) and smoothly interpolating it between 0.01 and 0.3 Hz. A choice of  $Q^{-1}(f) = 0.001$  at 0.01 Hz (e.g., Cormier 1982) changes the estimate of  $E_r$  generally by less than 10 %. The mean values of  $Q^{-1}(f)$ , shown by dots in the figure, and geometrical spreading of  $R^{-1/2}$  were used in normalizing observed spectra to a common distance of 2,000 km. Figure 9 shows the spectra of the four events (Z component) after this normalization. As expected, the spectra are reasonably similar. We note that the parameters used in normalization are



**Fig. 9** a Fourier acceleration spectra (Z component) of four earthquakes from Sumatra–Andaman region recorded at VISK (Table 1). The earthquakes have similar magnitudes and depths, but their epicentral distance varies between 1,610 and 2,262 km. The depth of one of the events is not available in Engdahl et al. (2007). It is indicated by a *question mark*. **b** Fourier acceleration spectra of the four earthquakes normalized to a common distance of 2,000 km



**Fig. 10**  $Q^{-1}(f)$  as a function of frequency. **a**  $Q^{-1}(f)$  for each event at selected frequencies  $(0.3 \le f \le 5 \text{ Hz})$ . Estimations from both horizontal and vertical components are included. **b** Mean and  $\pm 1$  standard deviation of  $Q^{-1}(f)$ .  $Q^{-1}(f)$  at 0.01 Hz is taken as 0.0067 (see text) and smoothly interpolated between 0.01 and 0.3 Hz



the same for all trajectories. Since this may introduce large error, caution must be exercised in comparing  $E_r$  when the trajectories are very different.

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